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TNSL20 - basic logistic algorithms

Homework Set 4, 2017

Solutions are due October 10, 2017.

Question 1 (IMPLEMENTATION): Implement the algorithm that tests if a given set of vertices I is an independent set for a given graph $G = (V, E)$ using the adjacency matrix of the graph.

Pseudocode of the algorithm is as follows:

Algorithm 1: Test for independence

Input : Adjacency matrix A , set of vertices I
Output: Boolean value t (true if I is an independent set and false otherwise)

```
1 Function is_independent_set ( $A, I$ )
2    $t := \text{true};$ 
3   if length( $I$ ) > 1 then
4     for  $v_{index} = 1$  TO length( $I$ )-1 do
5        $v := I[v_{index}];$ 
6       for  $w_{index} = v_{index} + 1$  TO length( $I$ ) do
7          $w := I[w_{index}];$ 
8         if  $A[v][w] == 1$  then
9            $t := \text{false};$ 
10        end
11      end
12    end
13  end
14  return  $t$ ;
15 end
```

Test your code on the adjacency matrix obtained from the Homework 2 Question 3 (b).

Question 2 (IMPLEMENTATION): Combine code from Homework 2 Question 3 and Homework 4 Question 1 in order to get a code that works with E and n as an input.

Algorithm 2: Test for independence

Input : Edges E , number of vertices n , set of vertices I

Output: Boolean value t (true if I is an independent set and false otherwise)

```
1 Function is_independent_set_without_adjacency_matrix ( $E, n, I$ )  
2   |  $A :=$  adjacency_matrix ( $E, n$ ) ;           // algorithm from HW2 Q3  
3   |  $t :=$  is_independent_set ( $A, I$ ) ;         // algorithm from HW4 Q1  
4   | return  $t$ ;  
5 end
```
